

# Dots and Boxes

Tamta and Anna are sisters who like playing a game of Dots and Boxes.

The game starts with an empty N + 1 by M + 1 grid of dots (and correspondingly, N by M grid of boxes). Players take turns adding a single horizontal or vertical edge between two *unjoined* adjacent dots (two dots are adjacent if the distance between them is 1). If a player completes the fourth side of a  $1 \times 1$  box on her turn she claims it, earns one point and **takes another turn**, otherwise the turn switches to another player. The game ends when no more edges can be placed.

Possible next three turns in a grid with N = 2, M = 3 (dotted lines are player moves):



Anna and Tamta have been playing for a while and you've noticed that in a current state **each box has exactly zero or two unjoined sides and it's Anna's turn to move.** (you can see an example in the image on the right. Note that image above does not fit this description).

The score of this game will be calculated as  $S_A - S_T$  where  $S_A$  is the number of points Anna earns from this point forward and  $S_T$  is the number of points that Tamta earns. Obviously, Anna is trying to maximize the score while Tamta is trying to minimize it. You need to calculate the final score knowing both players act optimally.



### Input

The first line contains two integers N and M which are number of rows and number of columns in a grid of boxes.

### EJOI 2020 Day 2

#### game (English)



Following *N* lines contain M + 1 digits in the same format, j-th number in i-th row is 1 if and only if there is a **vertical** edge between the dots with coordinates (i,j) and (i+1,j).

# Output

The only line should contain a single integer, the final score.

# Constraints

- $3 \le N, M \le 20$
- each box has exactly zero or two unjoined sides

# Subtasks

Let's define a component as a maximum set of unclaimed boxes on a grid such that you can move from any box to any other box by traversing the edges that aren't drawn yet. In the image you can see 5 different components.

- 1. (20 points): There is only a single component left in the game
- 2. (20 points):  $N \cdot M \le 12$
- 3. (20 points): There are only two components left in the game
- 4. (20 points):  $N \le 7, M \le 7$
- 5. (20 points): No additional constraints





# EJOI 2020 Day 2 game (English)



# Example

Input	Output
3 3	-5
000	
111	
011	
110	
1010	
1000	
1001	
55	6
00100	
10100	
11010	
00100	
01000	
11100	
011111	
001011	
101011	
110111	
100111	

The first example and one of the possible optimal move orders are depicted below (numbers on edges indicate turn order, red colors used by Anna and blue used by Tamta).

Second example is the one shown in the above pictures.

